

125 HW #8


4.2 7, 17

4.3 6,  $9ab$ ,  $38ab$

4.2 #7

on  $[0, 8]$ , MVT says there is some  $c$

with  $f'(c) = \frac{f(8) - f(0)}{8 - 0} = \frac{6 - 4}{8} = \frac{2}{8} = \frac{1}{4}$

This is a slope like , which seems to happen at  $c \approx .9, 3.1, 4.4, 6.1$

4.2 #17  $f(x) = 1 + 2x + x^3 + 4x^5$

$f(0) = 1$

$f(-1) = 1 - 2 - 1 - 4 < 0$

so by IVT,  $f(x)$  has a root.

Also,  $f'(x) = 2 + 3x^2 + 20x^4$

is always positive (even powers)

So  $f(x)$  is always increasing, so cannot have more than 1 root.

(Or, say that 2 roots means we get points  $a, b$  with  $f(a) = 0$  and  $f(b) = 0$ , so  $f(a) = f(b)$ . Then by Rolle, there is a pt with  $f'(x) = 0$ , which is a contradiction.)

4.3 #6a

$$f'(x) > 0 \text{ on } [0, 1), (3, 5)$$

so  $f$  is increasing there

$$f'(x) < 0 \text{ so } f \text{ is decreasing on } (1, 3) \text{ and } (5, 6]$$

4.3 #9ab

$$f(x) = 2x^3 + 3x^2 - 36x$$

$$f'(x) = 6x^2 + 6x - 36$$

$$\begin{aligned} \text{crit pts: } 6x^2 + 6x - 36 = 0 &\Rightarrow x^2 + x - 6 = 0 \\ &(x+3)(x-2) = 0 \\ &x = 2 \text{ or } -3. \end{aligned}$$

$$\begin{array}{ccccccc} & & -3 & & 2 & & \\ f' & & + & & - & & + \\ & & & & \uparrow & & \\ & & f'(-4) > 0 & & f'(1) < 0 & & f'(3) > 0 \end{array}$$

a) So  $f$  is inc. on  $(-\infty, -3)$  and  $(2, \infty)$   
 $f$  is dec. on  $(-3, 2)$

b)  $f(-3)$  is a local maximum  
 $f(2)$  is a local minimum.

4.3 #38ab

$$G(x) = x - 4\sqrt{x}$$

$$G'(x) = 1 - 2x^{-1/2} = 1 - \frac{2}{\sqrt{x}}$$

crit. pts:  $1 - 2x^{-1/2} = 0$

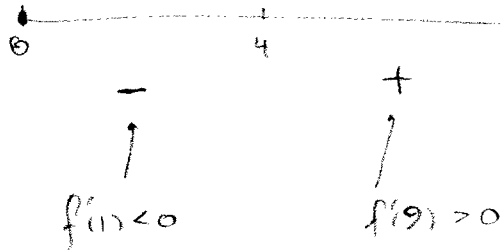
$$1 = 2x^{-1/2}$$

$$\frac{1}{2} = x^{-1/2}$$

$$\frac{1}{4} = x^{-1}$$

$$x = 4$$

$f''_0$



Also,  $G'(x)$  DNE at  $x=0$   
or  $x < 0$

a) So  $G$  is decreasing on  $(0, 4)$   
... .. increasing on  $(4, \infty)$

b)  $G(4)$  is a local minimum.

$G(0)$  is also a local max, since  
 $G(0) = 0$ , and then  $G$  decreases