

14	10	8	4	1	<u>points</u>
A	C	D	B	C	3
B	B	C	D	D	2
C	D	B	C	B	1
D	A	A	A	A	0

Using Borda

$$A: 14 \cdot 3 + 10 \cdot 0 + 8 \cdot 0 + 4 \cdot 0 + 1 \cdot 0 = 42$$

$$B: 14 \cdot 2 + 10 \cdot 2 + 8 \cdot 1 + 4 \cdot 3 + 1 \cdot 1 = 69 \leftarrow B \text{ wins}$$

$$C: 14 \cdot 1 + 10 \cdot 3 + 8 \cdot 2 + 4 \cdot 1 + 1 \cdot 3 = 67$$

$$D: 14 \cdot 0 + 10 \cdot 1 + 8 \cdot 3 + 4 \cdot 2 + 1 \cdot 2 = 44$$

Plurality, Condorcet, Borda

Which method is better?

We'll discuss various criteria for judging?

2 criteria based on the general idea:

a good system should choose
a solid popular candidate.

The Majority Criterion If there is a candidate who ranks first place on a majority of ballots, then they should win the election.

The Condorcet Winner Criterion (CWC)

If there is a Cond. winner, then they should win the election.

We would like a system to satisfy both of these.

Are they satisfied by plurality, Condorcet, Borda?

Plurality

Majority Crit "if a cand. gets top ranking on a majority, then they should win"

In plurality system, we count # of top rankings, so if they have a majority in top position, they will get the most votes in plurality.

So plurality does satisfy Majority criterion.

	Maj	CWC	
Plurality	✓	X	
Condorcet			
Borda	X	X	

Does plurality satisfy CWC? NO

sometimes a Cond winner can lose
if we use plurality.

Borda and Majority & CWC.

Borda: our 37 voters election:

A wins plurality

B wins Borda

C is Cond. winner

So Borda does not satisfy CWC.

Borda & Majority:

"if some candidate is top ranked by a majority, they should win"

This is not satisfied:

	<u>3</u>	<u>2</u>	here, A is top-ranked by a majority.
2	A	B	
1	B	C	Borda:
0	C	A	A: $3 \cdot 2 + 2 \cdot 0 = 6$
			B: $3 \cdot 1 + 2 \cdot 2 = 7$
			C: $3 \cdot 0 + 2 \cdot 1 = 2$

B wins!