## Math 1015: Homework #4

Question 1. Prove that dictatorship satisfies IIA.

Question 2. Please use this example election to show that Borda does not satisfy IIA:

4	3	3	2
Α	В	С	D
В	Α	D	Е
$\mathbf{C}$	$\mathbf{C}$	Α	С
D	D	В	А
Ε	Ε	Е	В

(Show how somebody can change their vote in a certain way that has a certain effect.)

Question 3. Consider this election, using plurality:

- a) Describe how the DACB voters can manipulate this election.
- b) Explain why the ACBD voters cannot manipulate this election.

**Question 4.** Three of our concepts involve people changing their votes and having certain effects: monotonicity, IIA, and manipulability. Say a sentence or two about each one describing the difference between these 3 things.