

Math 1172

Homework #4

6.4* #9a/8b, #50

6.6 #19, #62/64

6.4* #9a/8b

$$\log_{10} 40 + \log_{10} 2.5 = \log_{10} (40 \cdot 2.5)$$

$$= \log_{10} (100) = 2$$

(since $10^2 = 100$)

6.4* #50

$$\int \frac{2^x}{2^x + 1} dx$$

$$u = 2^x + 1$$

$$du = 2^x \ln 2 dx$$

$$\frac{1}{\ln 2} du = 2^x dx$$

$$\hookrightarrow \int \frac{2^x}{u} dx = \int \frac{1}{u} \cdot 2^x dx = \int \frac{1}{u} \cdot \frac{1}{\ln 2} du$$

$$= \frac{1}{\ln 2} \int \frac{1}{u} du = \frac{1}{\ln 2} \ln|u| + C$$

$$= \frac{1}{\ln 2} \ln|2^x + 1| + C$$

6.6 #19

$$\frac{d}{dx} (\cot^{-1} x)$$

$$y = \cot^{-1} x$$

$$\cot y = x$$

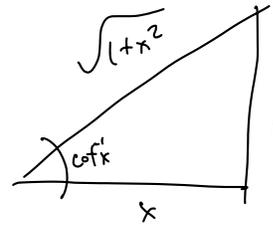
$$(\text{deriv. both sides}) \quad -\csc^2 y \frac{dy}{dx} = 1$$

$$\frac{dy}{dx} = -\frac{1}{\csc^2 y} = -\sin^2 y$$

$$= -(\sin(\cot^{-1} x))^2$$

$$= -\left(\frac{1}{\sqrt{1+x^2}}\right)^2 = -\frac{1}{1+x^2}$$

Stewart



6.6 # 62/64

$$\int_0^{\sqrt{3}/4} \frac{dx}{1+16x^2} = \int_0^{\sqrt{3}/4} \frac{dx}{1+(4x)^2}$$

$$u = 4x$$

$$du = 4dx$$

$$\frac{1}{4} du = dx$$

$$= \int \frac{1}{1+u^2} \cdot \frac{1}{4} du = \frac{1}{4} \int \frac{1}{1+u^2} du$$

$$= \frac{1}{4} \tan^{-1} u = \frac{1}{4} \tan^{-1}(4x) \Big|_0^{\sqrt{3}/4}$$

$$= \frac{1}{4} \tan^{-1}(\sqrt{3}) - \frac{1}{4} \tan^{-1}(0)$$

$$= \frac{1}{4} \pi/3 - \frac{1}{4} \cdot 0 = \pi/12$$

