

Math 1121 HW #8

Section 5.2 #14/18, 19/25

Section 5.3 #7/13, 29/35

5.2 #14/18

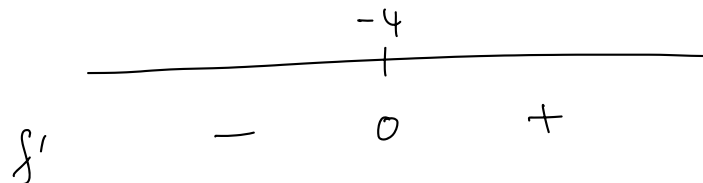
$$f(x) = x^2 + 8x + 5$$

$$f' = 0: \quad x+4=0$$

$$\quad \quad \quad x = -4$$

$$f'(x) = 2x + 8$$

$$= 2(x+4)$$



$$f'(-5) = 2(-5+4) = -$$

+ -

$$f'(0) = 2(0+4)$$

$x = -4$ is a rel. min.

5.2 #19/25

$$f(x) = x^4 - 18x^2 - 4$$

$$f'(x) = 4x^3 - 36x$$

$$= 4x(x^2 - 9)$$

$$= 4x(x-3)(x+3)$$

$$f' = 0:$$

$$4x = 0$$

$$x = 0$$

$$x-3 = 0$$

$$x = 3$$

$$x+3 = 0$$

$$x = -3$$

$$\begin{array}{ccccccc}
 & & -3 & & 0 & & 3 \\
 & & | & & | & & | \\
 f' & & - & 0 & + & 0 & - & 0 & +
 \end{array}$$

$$f'(-4) = 4(-4)(-4-3)(-4+3) \quad f'(1) = 4(1)(1-3)(1+3)$$

$$\begin{array}{cccc}
 + & - & - & - \\
 + & + & - & +
 \end{array}$$

$$f'(-1) = 4(-1)(-1-3)(-1+3) \quad f'(4) = 4(4)(4-3)(4+3)$$

$$\begin{array}{cccc}
 + & - & - & + \\
 + & + & + & +
 \end{array}$$

$x = -3$ is a rel min

$x = 0$ is a rel max

$x = 3$ is a rel min

5.3 #7/13

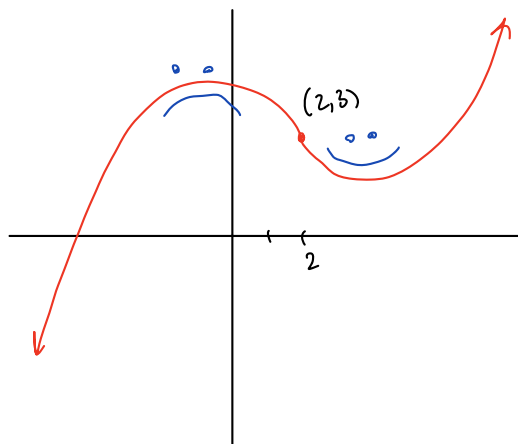
$$f(x) = \frac{x^2}{1+x}$$

$$f'(x) = \frac{(1+x) \cdot 2x - x^2 \cdot (1)}{(1+x)^2} = \frac{2x + 2x^2 - x^2}{(1+x)^2}$$

$$f'(x) = \frac{2x + x^2}{1 + 2x + x^2}$$

$$f''(x) = \frac{(1+2x+x^2) \cdot (2+2x) - (2x+x^2)(2+2x)}{(1+2x+x^2)^2}$$

5.3 #29/35



conc. up on $(-\infty, 2)$
conc. down on $(2, \infty)$

$(2, 3)$ is an inflection pt.