

Exam 1 Practice

#1

4	2	3	
A	B	C	A: 4
B	C	B	B: 2
C	A	A	C: 3

A wins plurality

#2

Round 1:

A: 4	
B: 2	
C: 3	

Round 2:

4	2	3	
A	C	C	A: 4
C	A	A	<u>C: 5</u>

C wins RCV

#3

A \vee B: A: 4
B: 2+3 = 5

A \vee C: A: 4
C: 2+3 = 5

B \vee C: B: 4+2 = 6
C: 3

B wins Condorcet

#4

4	2	3	
A	B	C	2
B	C	B	1
C	A	A	0

A: $4 \cdot 2 + 0 + 0 = 8$

B: $4 \cdot 1 + 2 \cdot 2 + 3 \cdot 1 = 4 + 4 + 3 = 11$

C: $0 + 2 \cdot 1 + 3 \cdot 2 = 2 + 6 = 8$

B wins Borda.

#5 Even if one candidate is ranked 1st by a majority,
the dictator may choose someone else to win.
So the majority winner may not actually win
in a dictatorship

#6

4	3	2
A	C	B
C	A	C
B	B	A

OG results: A: 4
B: 2
C: 3

A wins.

The $\begin{smallmatrix} B \\ C \\ A \end{smallmatrix}$ voters hate this outcome. They can change

to $\begin{smallmatrix} C \\ B \\ A \end{smallmatrix}$. Then it looks like:

4	3	2
A	C	C
C	A	B
B	B	A

A: 4
B: 0
C: 5

C wins!

This is a preferable outcome for those voters,
so this is a manipulation.

#7 This is not the same. "Random dictator" chooses a
ballot at random, which means a candidate with more
votes is more likely to be chosen.
That's different from just choosing the winner
at random, which would make all outcomes equally likely.

#8

It would be:

	3	4	2
A	✓	✓	
B		✓	✓
C			✓
D	✓		

A: 7

B: 6

C: 2

D: 3

A wins

#9

Many possible answers

a) $[5: 6, 1, 1]$

b) $[10: 7, 7, 1, 1]$ the 1's are both dummies

c) $[10: 7, 7, 1, 1]$ each 7 has veto power,
but neither is a dictator.

#10

$$[15: \begin{matrix} A & B & C \\ 12 & 10 & 3 \end{matrix}]$$

perms	weights	pivotal
A B C	12 (10) 3	B
A C B	12 (3) 10	C
B A C	10 (12) 3	A
B C A	10 3 (12)	A
C A B	3 (12) 10	A
C B A	3 10 (12)	A

$$\begin{aligned} A &: 4/6 \\ B &: 1/6 \\ C &: 1/6 \end{aligned}$$