

Math 1015 HW #3

#2, 3b, 5a, 7

#2 RCV satisfies the Majority Winner Crit.

Proof Imagine X is ranked 1st place by a majority of voters. Then X will always have a majority of 1st place votes in every round, so X is never eliminated.

Therefore X wins using RCV.

#4b We need an example where someone is ranked last by a majority of voters, but still wins:

<u>5</u>	<u>5</u>	<u>6</u>
A	B	C
B	A	A
C	C	B

Here C wins with plurality, even though 10 out of 16 voters ranked C last.

#5a

<u>2</u>	<u>4</u>	<u>3</u>
A	B	D
C	A	A
B	D	C
D	C	B

Using plurality, OG winner is B.

The $\begin{matrix} D \\ A \\ C \\ B \end{matrix}$ voters should instead say $\begin{matrix} A \\ D \\ C \\ B \end{matrix}$. Then it would

look like:

<u>2</u>	<u>4</u>	<u>3</u>
A	B	A
C	A	D
B	D	C
D	C	B

Now A wins, which is preferable in their opinion because they like A better than B.

#7

375	282	85	83	82	47	35	31	29	→ Total: 1649
M	C	L	M	C	C	L	L	M	
L		M		L	M		C	C	

$$M: 375 + 83 + 29 = 487$$

$$C: 282 + 82 + 47 = 411$$

$$L: 85 + 35 + 31 = 151$$

$$M: 487/1649 = 46.47\%$$

$$C: 411/1649 = 39.2\%$$

$$L: 151/1649 = 14.4\%$$